# Modeling Performance of Graph Programs on GPUs in a Compiler

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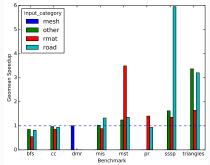
Queuing Models for Graph Programs

Results, Analytical Modelling and Characterization

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#### Speedup of the Galois GPU compiler on 7 graph algorithms<sup>1</sup>



<sup>1</sup>S. Pai and K. Pingali, ``A compiler for throughput optimization of graph algorithms on GPUs", in *OOPSLA 2016*.

## Performance of Graph Programs

- Algorithm
  - BFS is O(|V + E|), but many implementations are  $O(n^2)$
  - +  $\delta\text{-stepping SSSP}$  is an order of magnitude faster than naive
- Graph Input
  - Road networks are uniform, high-diameter, and exhibit locality
  - Social network graphs are non-uniform, low-diameter and have little locality
- Software (Runtime)
  - Data structure memory layout
  - Data structure implementation
- Hardware
  - Memory bandwidth (?)
  - Atomic instruction performance

- $\cdot\,$  No performance model exists for graph programs on GPUs
  - Must manually tease out performance effects
- No sound methodology exists to guide effort
  - Ad hoc techniques lead to incorrect generalizations
- No useful characterization to drive algorithms, runtimes, architecture
  - Can we ever achieve peak performance?

## Queuing Models for Graph Programs

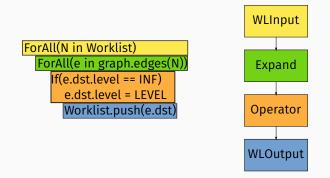
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```
Level-by-Level Breadth-First Search (BFS)
```

```
Kernel BFS(graph, LEVEL)
ForAll(N in Worklist)
ForAll(e in graph.edges(N))
If(e.dst.level == INF)
e.dst.level = LEVEL
Worklist.push(e.dst)
```

- Worklist contains source node initially
- Worklists are bulk-synchronous

## BFS as a Queuing Model

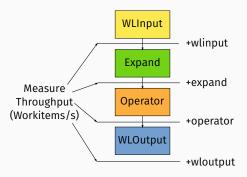


Except for Operator, all other stages are independent of BFS

The Operator Machine is a multistage queuing network model for graph programs:

- Input
  - WLINPUT, ALLNODESINPUT, ALLEDGESINPUT
- Expansion (optional)
  - XSerial, XThreadBlock, XWarp, ...
- Operator
  - NodeOp, EdgeOp
- Output (optional)
  - WLOUTPUT

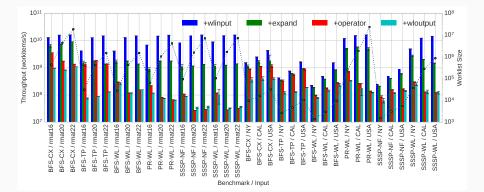
- "Cumulative" benchmarks for each stage
- Requires checkpoints from full executions
  - Compiler-assisted
- Yields peak throughputs



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### Initial Results: Peak Throughputs



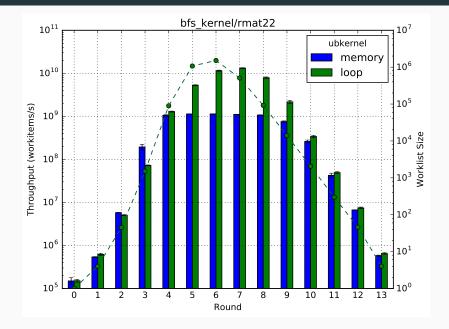
## Input Performance

- WLINPUT Read a worklist
- Peaks out at 56GByte/s
- Depends on:
  - Size of worklist
  - Number of concurrent reads / thread
- Worklists are large for Social Network Graphs
- Worklists are usually small for Road Networks
  - In BFS and SSSP
  - Not in PageRank, Minimum Spanning Tree, Connected Components

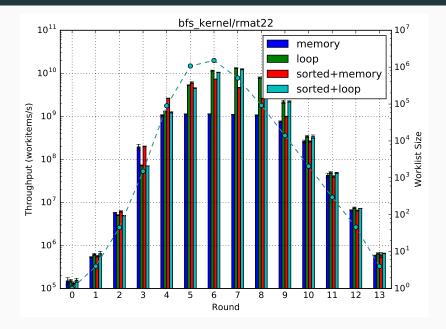
Assuming graph data-structure uses CSR layout

```
N = Worklist[tid]
// indirect memory accesses
start = graph.row_offset[N];
end = graph.row_offset[N+1];
// irregular loop
for(i = start; i < end; i++) {
    // empty
}</pre>
```

### Microbenchmark Performance for Expansion



# After sorting the worklist



- Indirect Memory Access performance is dictated by:
  - Number of 32-byte lines spanned per GPU warp
  - TLB hit rate
- Loop performance is dictated by:
  - Maximum number of edges
  - Branch performance

Queuing Models for Graph Programs

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- Operator Machine is a queuing network model for graph programs on GPUs
  - Allows us to drill down into performance
  - Generalizes well
  - Yields sound conclusions
- TLB Miss Throughput is critical for random graphs
- Compiler integration in progress to guide profile-based optimizations